

AAL, Ex. 5.

1. Calculate $\gamma_i(D_n)$.
2. Calculate the commutator subgroup of S_n .
3. Prove that the commutator $[\pi, \sigma]$ is a 3-cycle if $|\text{supp}(\pi) \cap \text{supp}(\sigma)| = 1$.
4. Show that the 3-cycles generate A_n .
5. Let G be a group of order pq , where p and q are primes. Prove that G is solvable.
6. Show that a subgroup of a nilpotent group is maximal if and only if it has prime index.